

Calculus 1 First



Palestine Technical University
Mathematics Department.

~~Linear Algebra I (Math 122)~~

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First Exam

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معن سدرام قنطان

Student name بالعربية:

Student #

RTN 11:00 - 11:50

I: (36 points) Choose the correct answer.

1. The solution of the inequality $\left|\frac{2}{x} - 4\right| < 1$ is

a) $\left(\frac{2}{5}, \frac{2}{3}\right)$

b) $\left(\frac{3}{2}, \frac{7}{2}\right)$

c) $\infty - \left(\frac{2}{5}, \frac{2}{3}\right)$

d) $\infty - \left(\frac{3}{2}, \frac{7}{2}\right)$

$$-1 < \frac{2}{x} - 4 < 1$$

$$+4 \quad +4 \quad +4$$

$$3 < \frac{2}{x} < 5$$

$$\frac{1}{3} > \frac{x}{2} > \frac{1}{5}$$

$$\frac{2}{5} < x < \frac{2}{3}$$

$$\frac{2}{3} > x > \frac{2}{5}$$

2. If $\lim_{x \rightarrow 0^+} (4g(x))^{\frac{1}{3}} = 2$, then $\lim_{x \rightarrow 0^+} g(x) =$

a) 8

b) 4

c) 2

d) -2

$$\sqrt[3]{4x} = 2$$

$$4x = 8$$

$$x = \frac{8}{4} = 2$$

3. $\lim_{x \rightarrow \infty} \frac{\cos x - 1}{x} =$

a) ∞

b) 1

c) D.N.E.

d) 0

$$\lim_{x \rightarrow \infty} \frac{\cos x - 1}{x} \left(\frac{\cos x + 1}{\cos x + 1} \right) = \frac{\cos^2 x - 1}{x(\cos x + 1)} = \frac{\sin^2 x + \cos^2 x - 1}{x(\cos x + 1)} = \frac{-\sin^2 x}{x(\cos x + 1)}$$

$$= \frac{-\sin x}{x} \cdot \frac{\sin x}{\cos x + 1} = 0 = \text{d}$$

4. Let $f(x) = \frac{1}{x-1}$, and $g(x) = \sqrt{x} + 1$, then the domain of the function $(f \circ g)(x)$ is

a) $[0, \infty)$

b) $(0, 1) \cup (1, \infty)$

c) $(0, \infty)$

d) $(-\infty, 0) \cup (0, \infty)$

$$\frac{1}{x-1} \Rightarrow x-1 \neq 0 \Rightarrow x \neq 1 \quad x \geq 1$$

$$f(g(x)) = \frac{1}{(\sqrt{x}+1)-1} = \frac{1}{\sqrt{x}} = \left(\frac{1}{\sqrt{x}}\right) \quad y \neq 0$$

5. The vertex of the parabola $-2x^2 + 4x + 1$ is

a) (0, 1)

b) (3, -5)

c) (2, 1)

d) (1, 3)

$$\frac{-b}{2a} = \frac{-4}{2(-2)} = \frac{-4}{-4} = 1$$

$$f(1) = -2(1)^2 + 4(1) + 1$$

$$= -2 + 4 + 1$$

$$= 2 + 1 = 3$$

$$\begin{array}{r} 30 \\ 4 \\ \hline 14 \\ 48 \end{array}$$

تم الرفع بواسطة معن أبو عيسى

6. The function $f(x) = x^3 - 2x + 2$ has

- ☒ a) a zero between -2 and 0.
☐ b) a zero between 2 and 3.
☐ b) no roots.
☐ d) no y intercepts.

$$\begin{aligned} &(-2)^3 - 2(-2) + 2 \\ &= -8 + 4 + 2 \\ &= -2 \end{aligned}$$

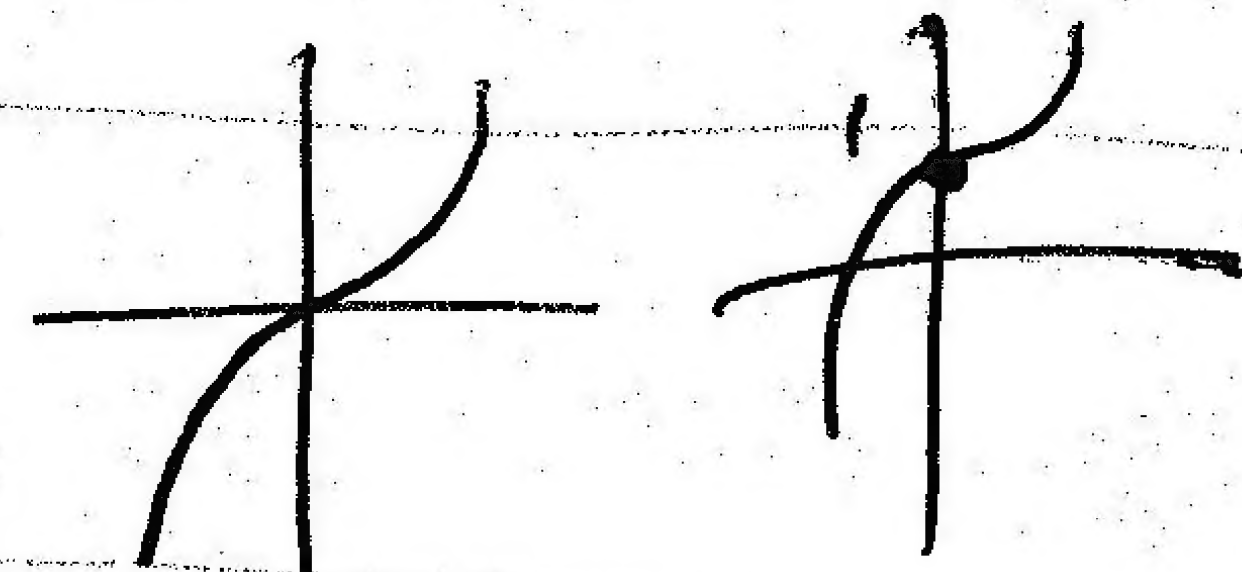
$[-2, 0]$

have zero between $(-2, 0)$

7. If f is odd and $\lim_{x \rightarrow 0^-} f(x) = 1$, then $\lim_{x \rightarrow 0^+} f(x) =$

- ☐ a) 1.
☒ b) -1.
☐ c) 0.
☐ d) else.

$$f(-x) = -f(x)$$



8. The graph of the equation $x^2 + y^2 - 4x - 6y - 3 = 0$ is

- ☒ a) a circle centered at (2, 3) and radius 4.
☐ b) a circle centered at (-2, 3) and radius 3.
☐ c) a circle centered at (-2, 3) and radius 4.
☐ d) an ellipse centered at (2, 3).
☐ e) an ellipse centered at (-2, 3).

$$(x^2 - 4x + 4) + (y^2 - 6y + 9) = 4 + 9 + 3$$

$$(x - 2)^2 + (y - 3)^2 = 16$$

(2, 3) radius 4

9. Let $f(x) = \begin{cases} \sqrt{-x} & -4 \leq x \leq 0 \\ \sqrt{x} & 0 < x < 4 \end{cases}$. Then, the range of f is

- ☐ a) $[-4, 4]$
☐ b) $[-2, 2]$
☒ c) $[0, 2]$
☐ d) $[0, 2]$.

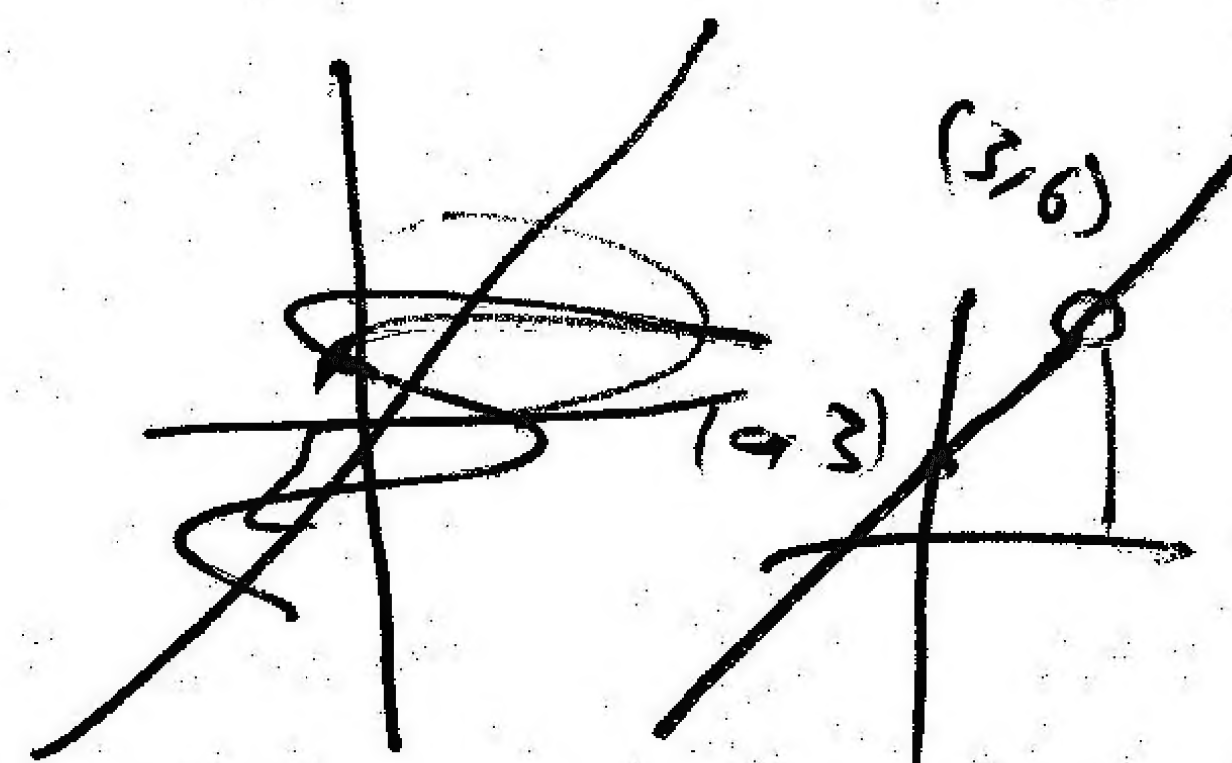
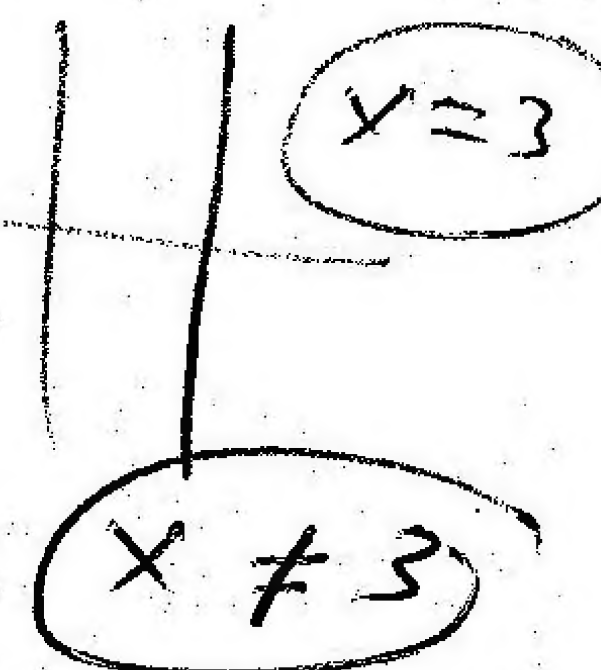
$$[0, 2]$$

10. At $x = 3$, the function $f(x) = \frac{x^2 - 9}{x - 3}$ has

- ☒ a) infinite discontinuity.
☒ b) a removable discontinuity.
☐ c) a jump discontinuity.
☐ d) a horizontal asymptote.

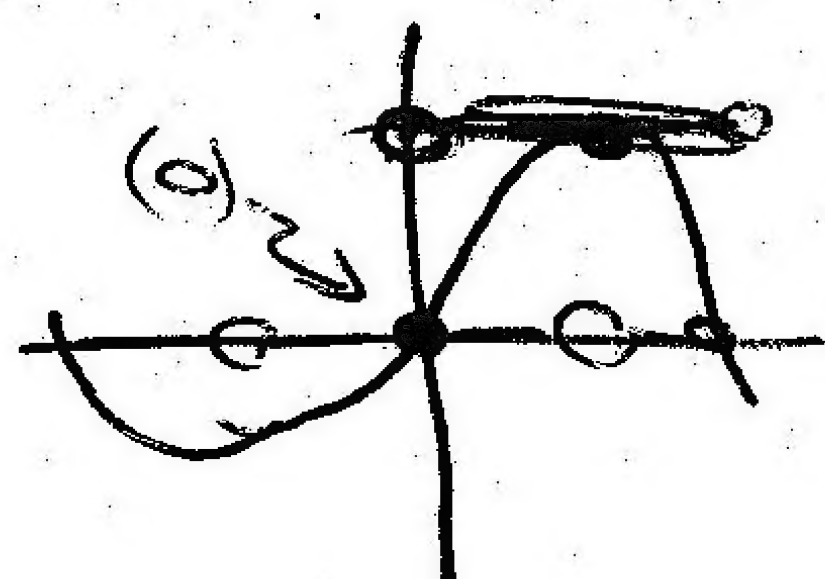
$$\frac{(x-3)(x+3)}{x-3}$$

$$f(3) = 3+3 = 6$$



11. $\lim_{x \rightarrow 0^+} \sin|x| =$

- ☒ a) 0
☒ b) 1
☐ c) -1
☐ d) DNE.



12. The equation of the line that passes through (1, -1) and normal to the line $y = 3x + 9$ is

- ☐ a) $y = x + 2$.
☐ b) $y = -x - 4$.
☒ c) $3y + x + 2 = 0$.
☐ d) $y = 4 - x$.

$$y = 3x + 9$$

$$m_1 = 3$$

$$m_1 m_2 = -1$$

$$3 m_2 = -1 \Rightarrow$$

$$m_2 = -\frac{1}{3}$$

$$Y - Y_0 = m(X - X_0)$$

$$2 \quad 3y + x + 2 = 0$$

$$Y - -1 = -\frac{1}{3}(X - 1)$$

$$3Y = -X + 2$$

$$Y + 1 = -\frac{1}{3}X + \frac{1}{3}$$

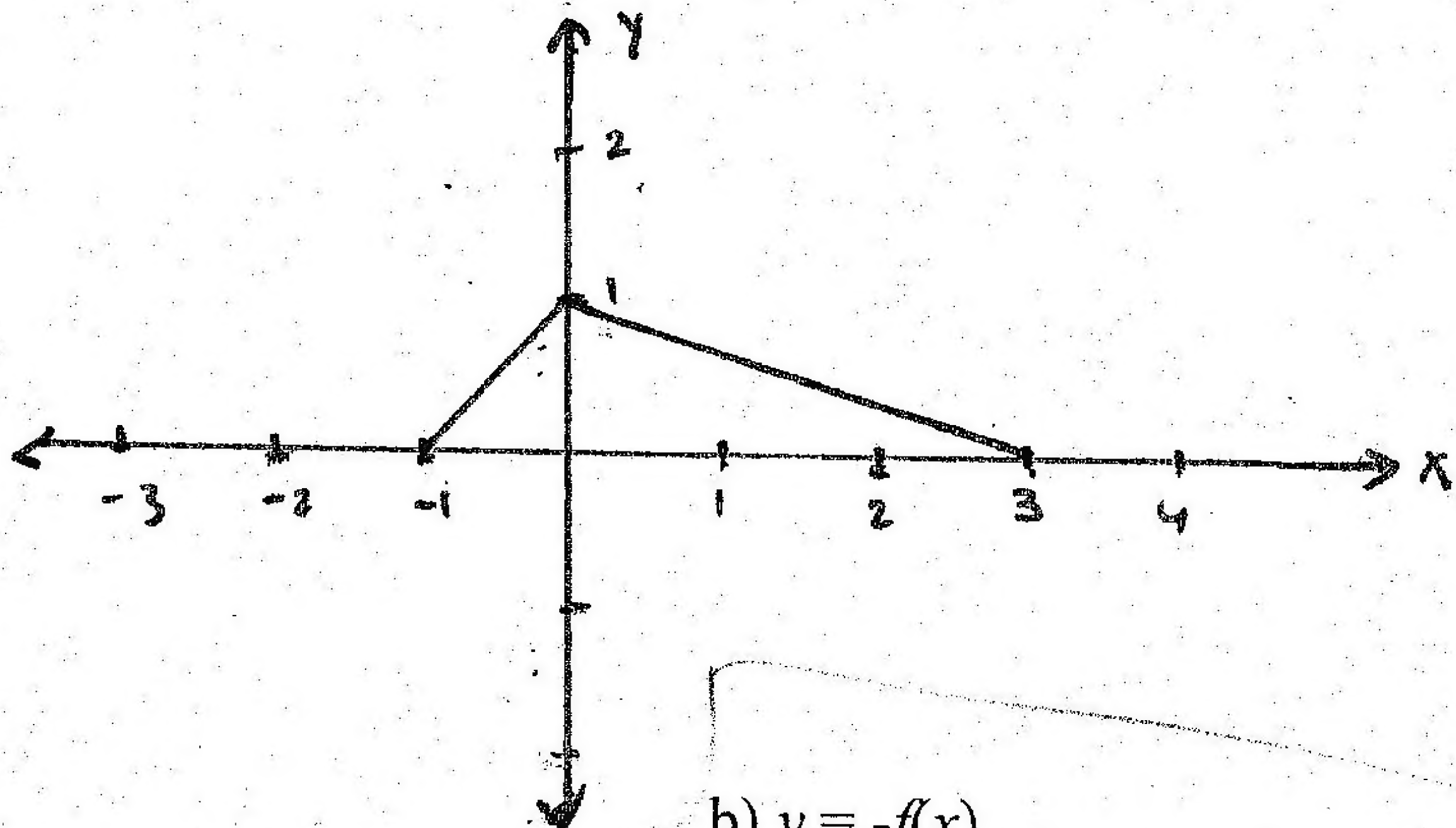
$$\Rightarrow Y = -\frac{1}{3}X - \frac{2}{3}$$

$$\times \times 3 \hookrightarrow$$

II

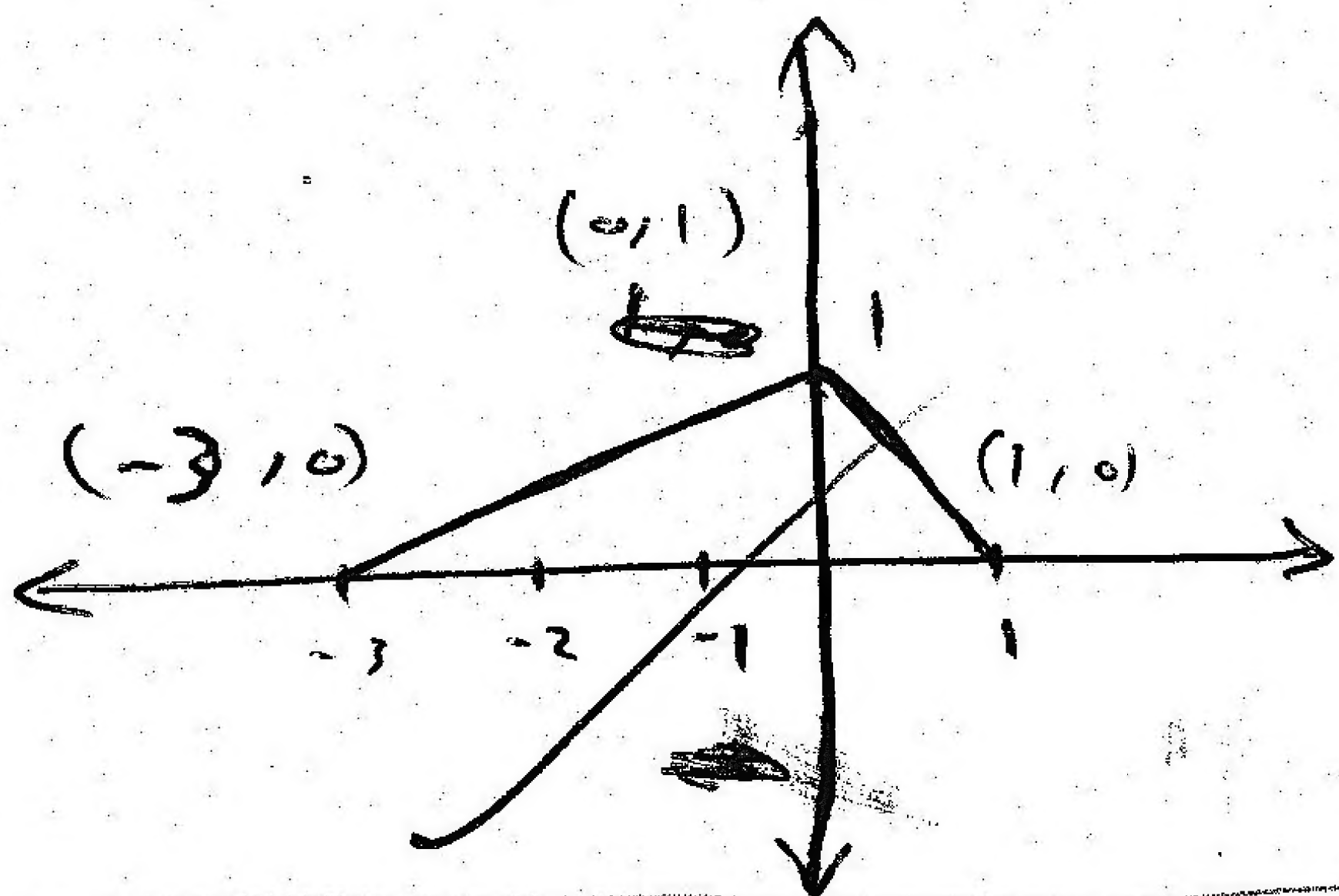
1. The graph of f is shown. Draw the graph of each function

(10 points)



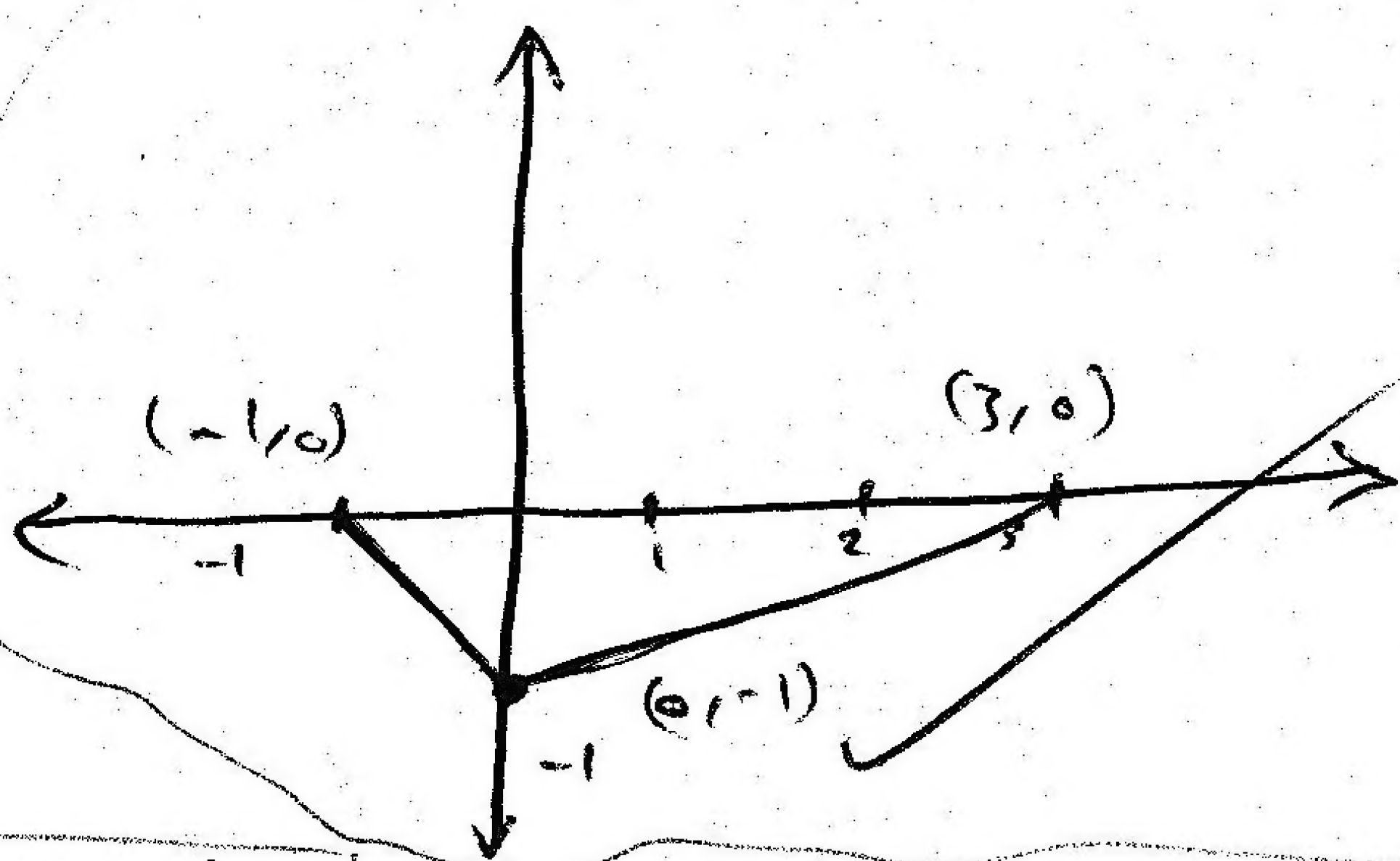
a) $y = f(-x)$.

reflection about y -axis



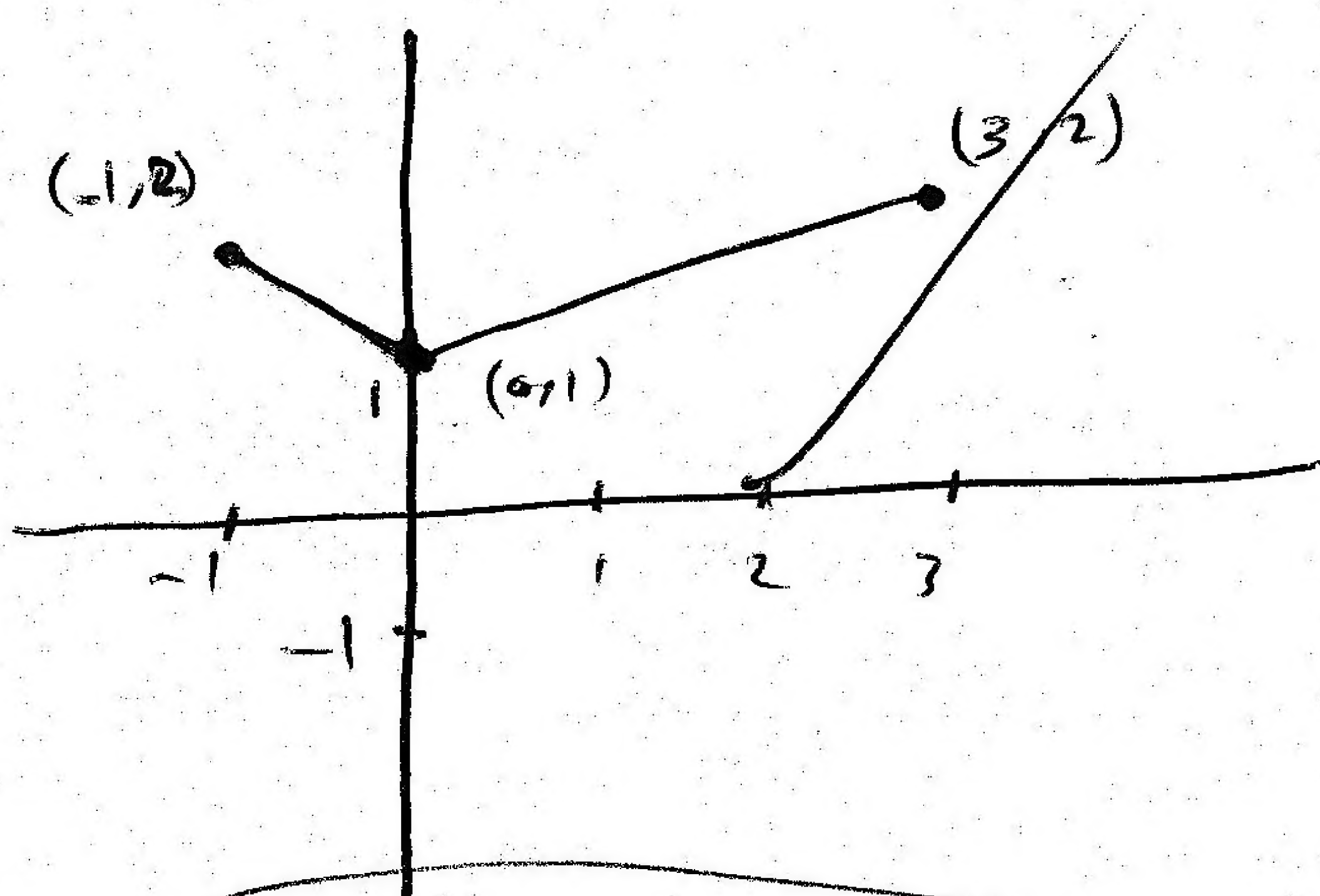
b) $y = -f(x)$

reflection about x -axis



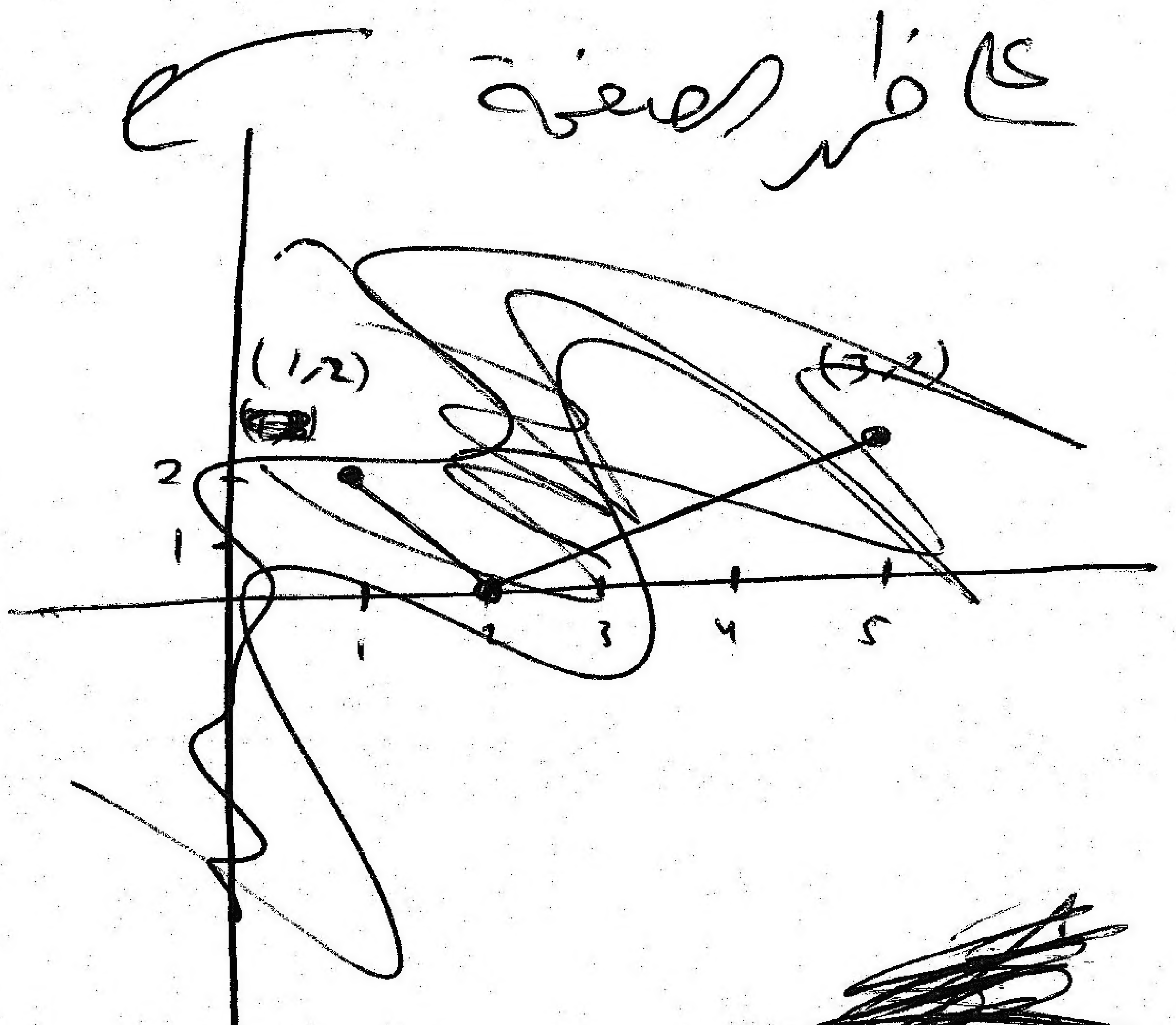
c) $y = 2 - f(x)$

$y = -f(x) + 2$



reflection about x -axis
and shifts 2 units above

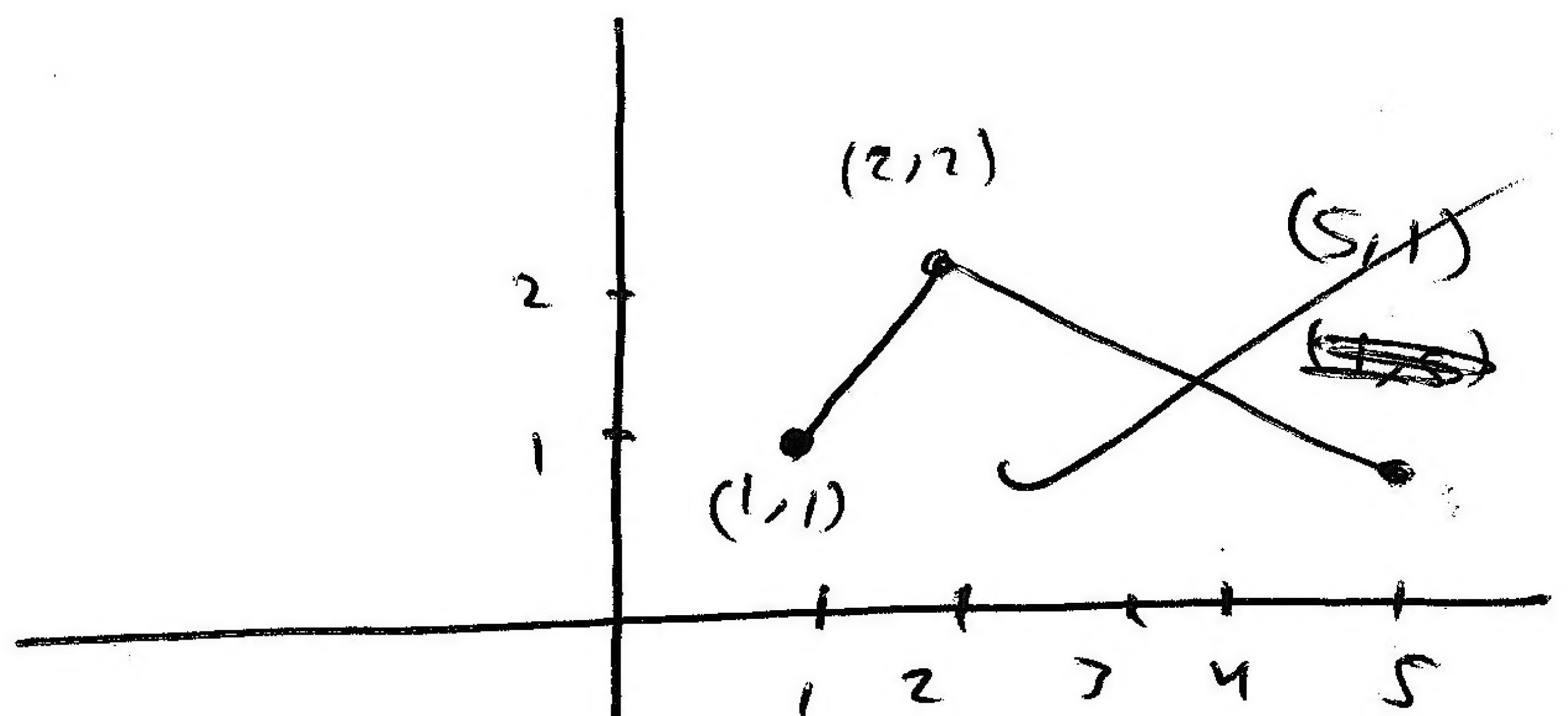
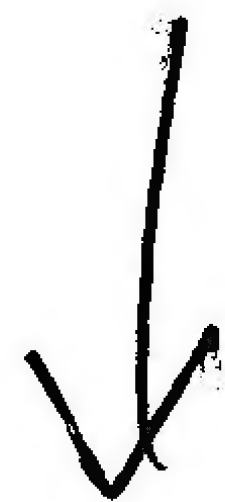
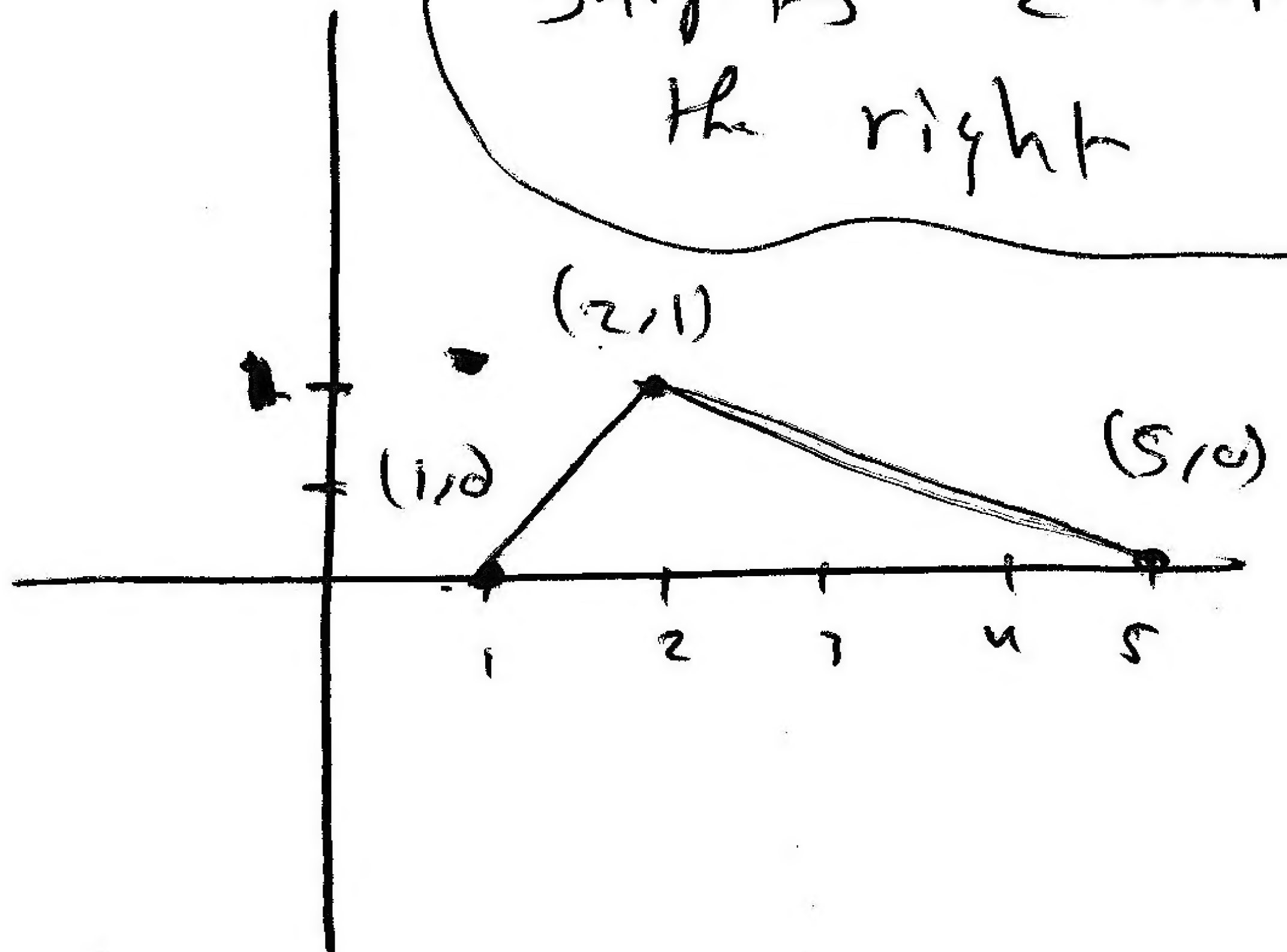
d) $y = f(x-2) + 1$



~~Shifts 2 units right and 1 unit up~~
~~Shifts 4 units right and 1 unit up~~

d

shifts 2 units to the right



then:

shifts 1 unit ~~to~~ above

2. Consider the function $f(x) = \frac{2x+3}{x+1}$.

(14 points)

a) Find the functions' x and y intercepts.

X-intercept $\Rightarrow x=0 \Rightarrow y=0$
 $\Rightarrow 2x+3=0 \Rightarrow x = -\frac{3}{2}$
 $\frac{2x+3}{x+1} = 0 \Rightarrow \left(-\frac{3}{2}, 0\right)$

Y-intercept $\Rightarrow x=0 \Rightarrow x+1=1$
 $= 3$
 $\frac{2(0)+3}{0+1} = \frac{3}{1}$
 $(0, 3)$

b) $\lim_{x \rightarrow \infty} f(x) = \frac{2x+3}{x+1} = \frac{\frac{2x}{x} + \frac{3}{x}}{\frac{x}{x} + \frac{1}{x}} = \frac{2+0}{1+0} = 2$

c) $\lim_{x \rightarrow -\infty} f(x) = \frac{2x+3}{x+1} = \frac{\frac{2x}{x} + \frac{3}{x}}{\frac{x}{x} + \frac{1}{x}} = \frac{2+0}{1+0} = 2$

d) $\lim_{x \rightarrow -1^+} f(x) = \frac{2x+3}{x+1} = +\infty$

e) $\lim_{x \rightarrow -1^-} f(x) = \frac{2x+3}{x+1} = -\infty$

f) The equation of the horizontal asymptote (if exists) is $y=2$

g) The equation of the vertical asymptote (if exists) is $x=-1$

h) Sketch the graph of f .

